

1.021, 3.021, 10.333, 22.00 : Introduction to Modeling and Simulation : Spring 2012

Part II – Quantum Mechanical Methods : Lecture 10

Solar PV

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Part II Topics

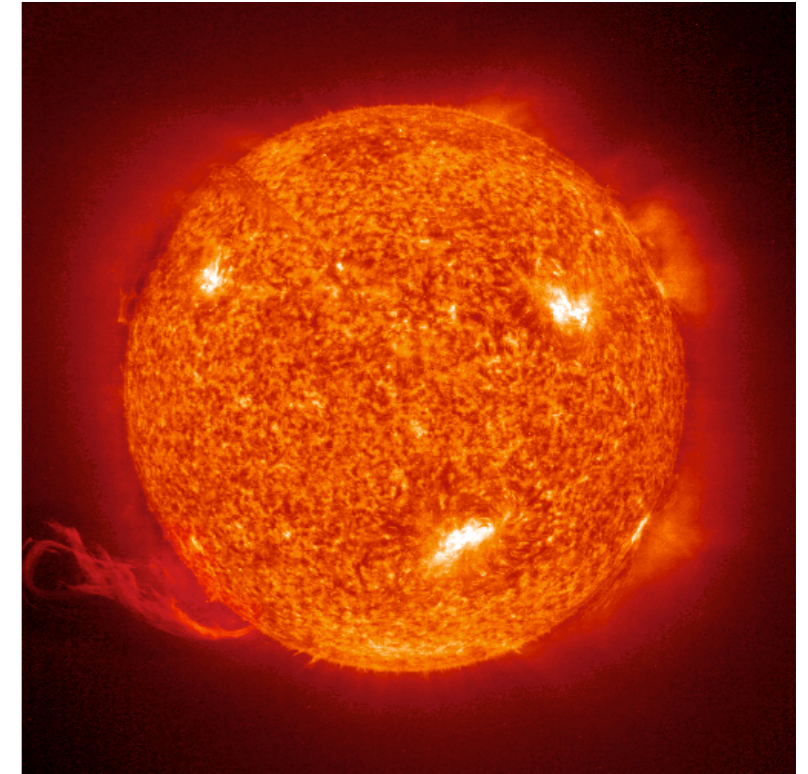
1. It's a Quantum World: The Theory of Quantum Mechanics
2. Quantum Mechanics: Practice Makes Perfect
3. From Many-Body to Single-Particle; Quantum Modeling of Molecules
4. Application of Quantum Modeling of Molecules: Solar Thermal Fuels
5. Application of Quantum Modeling of Molecules: Hydrogen Storage
6. From Atoms to Solids
7. Quantum Modeling of Solids: Basic Properties
8. Advanced Prop. of Materials: What else can we do?
9. Application of Quantum Modeling of Solids: Solar Cells Part I
10. Application of Quantum Modeling of Solids: Solar Cells Part II
11. Application of Quantum Modeling of Solids: Nanotechnology

Summary

- A bit of discussion of PSET 6
- Solar PV - More Motivation
- Solar PV - the viewpoint of the electron!
- How computational quantum mechanics can impact solar PV

Energy from the Sun

- Energy released by an earthquake of magnitude 8 (10^{17} J):
 - the sun delivers this in one second
- Energy humans use annually (10^{20} J):
 - sun delivers this in one hour
- Earth's total resources of oil (3 trillion barrels, 10^{22} J):
 - the sun delivers this in two days

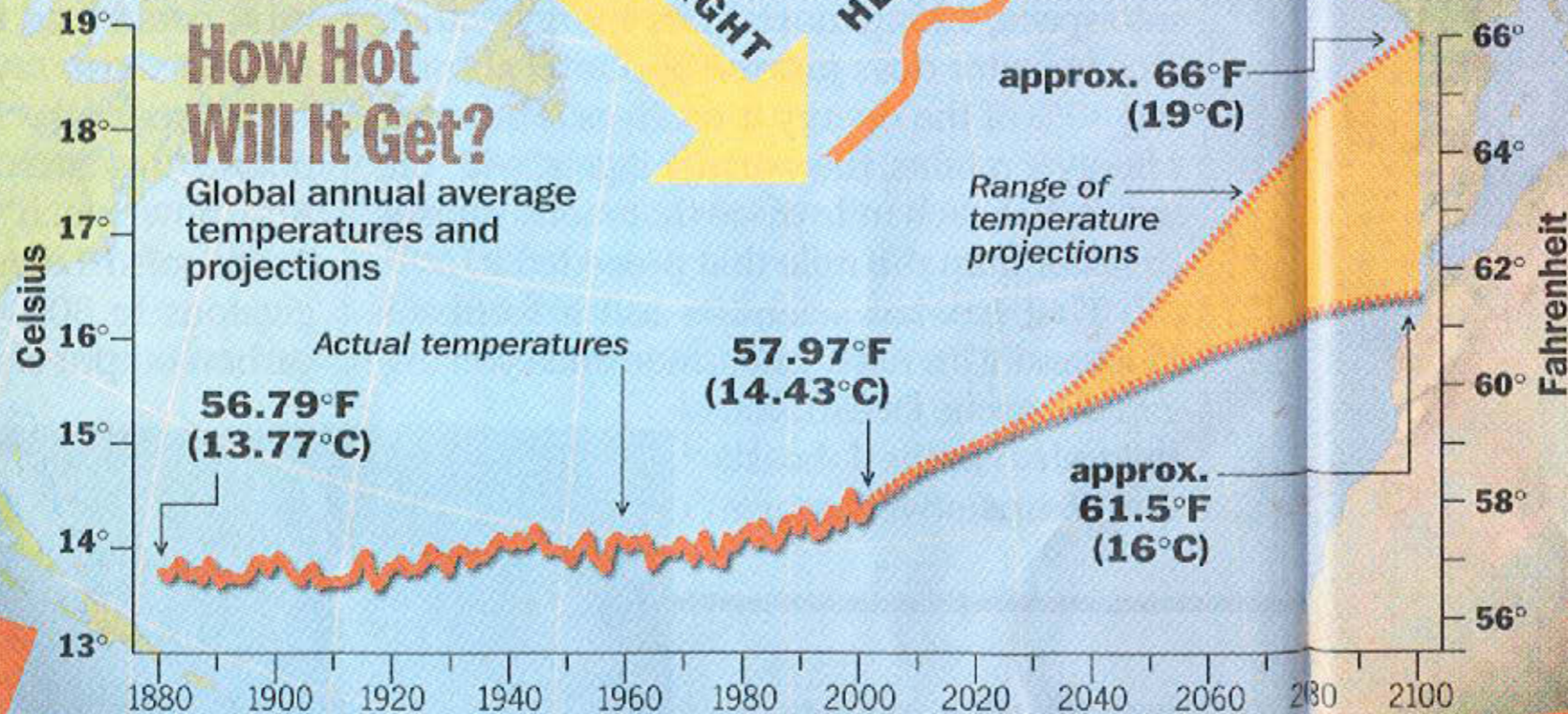


Courtesy of [SOHO/EIT](#) (ESA & NASA) consortium.

THE GREENHOUSE EFFECT

Without the **greenhouse effect**, life on Earth would not be possible. Energy from the sun is absorbed by the planet and radiated back out as heat. Atmospheric gases like **carbon dioxide** trap that heat and keep it from leaking into space. That's what keeps us warm at night.

But as humans pour ever increasing amounts of greenhouse gases into the atmosphere, more of the sun's **heat gets trapped**, and the planet gets a fever



Cost of Inaction?

Grinnell Glacier and Grinnell Lake, Glacier National Park, 1910-1997

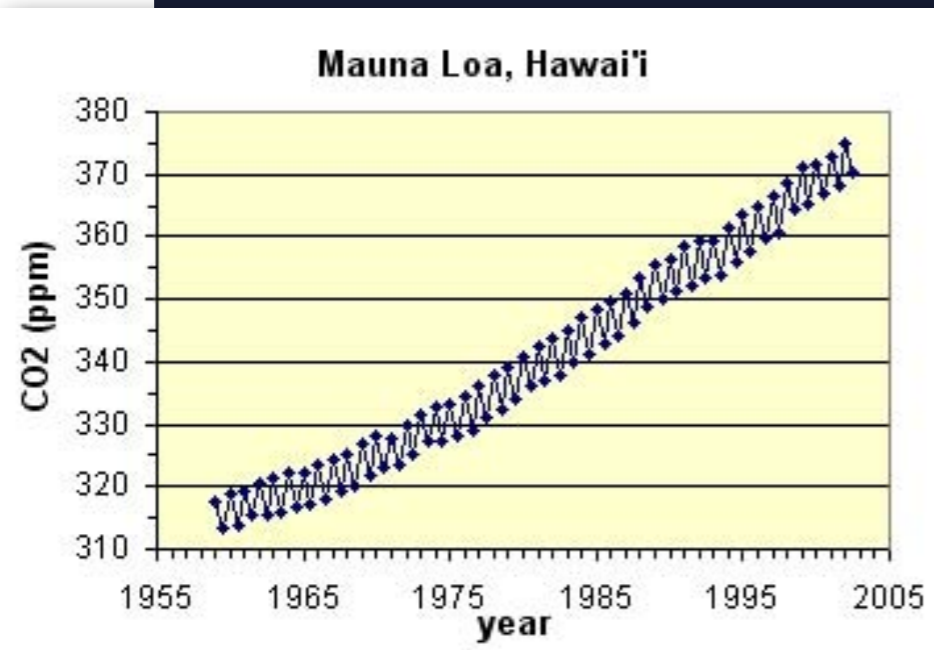
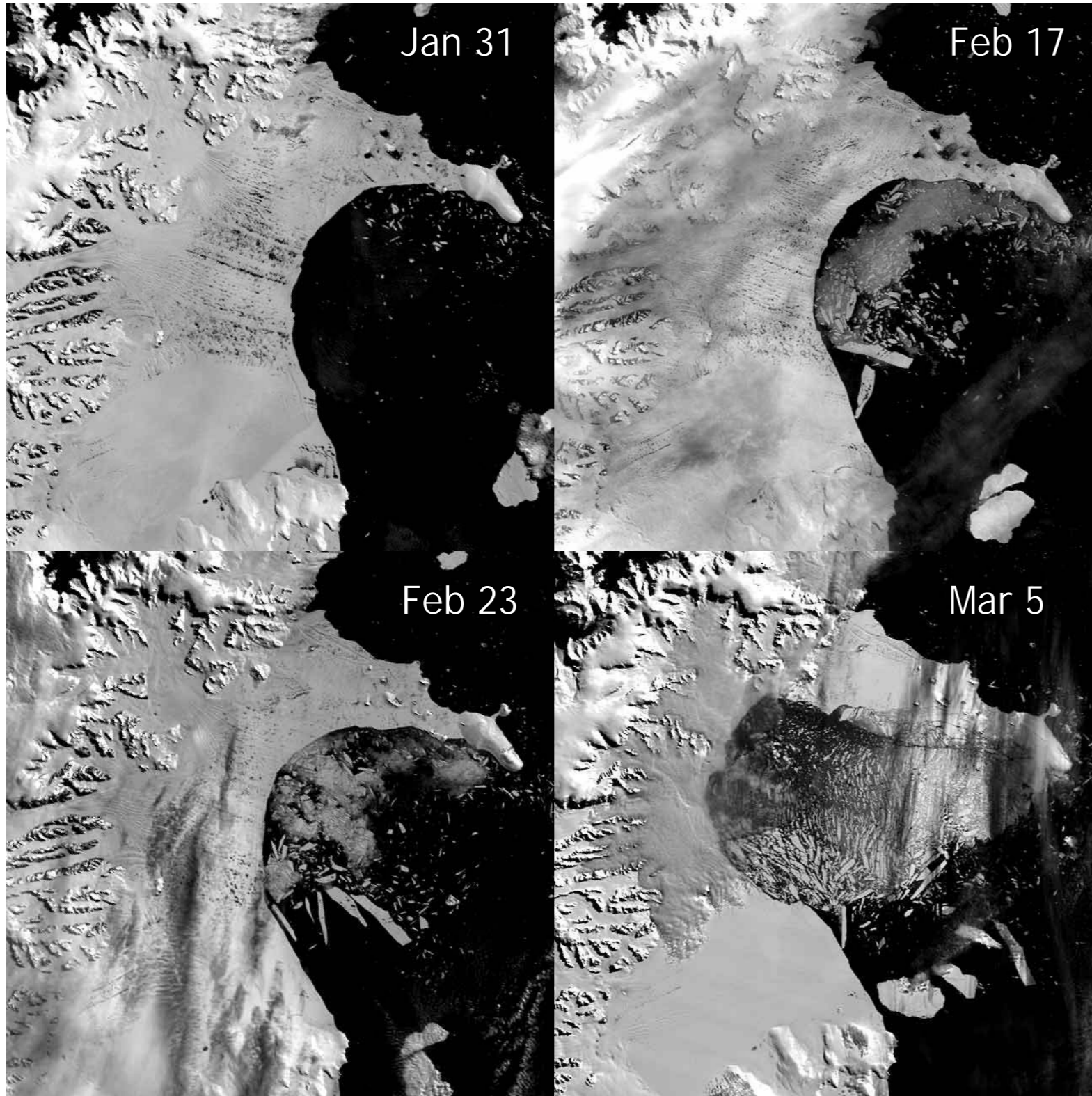


Image by Dr. Pieter Tans, [NOAA/ESRL](#) and Dr. Ralph Keeling, [Scripps Institute of Oceanography](#).


Warming is Real and Has Real Effects



Between Jan 31, 2002 and March 5, 2002 a chunk of the Larsen B ice shelf the size of Rhode Island disintegrated.

Images from NASA's Terra satellite, National Snow and Ice Data Center, University of Colorado, Boulder.

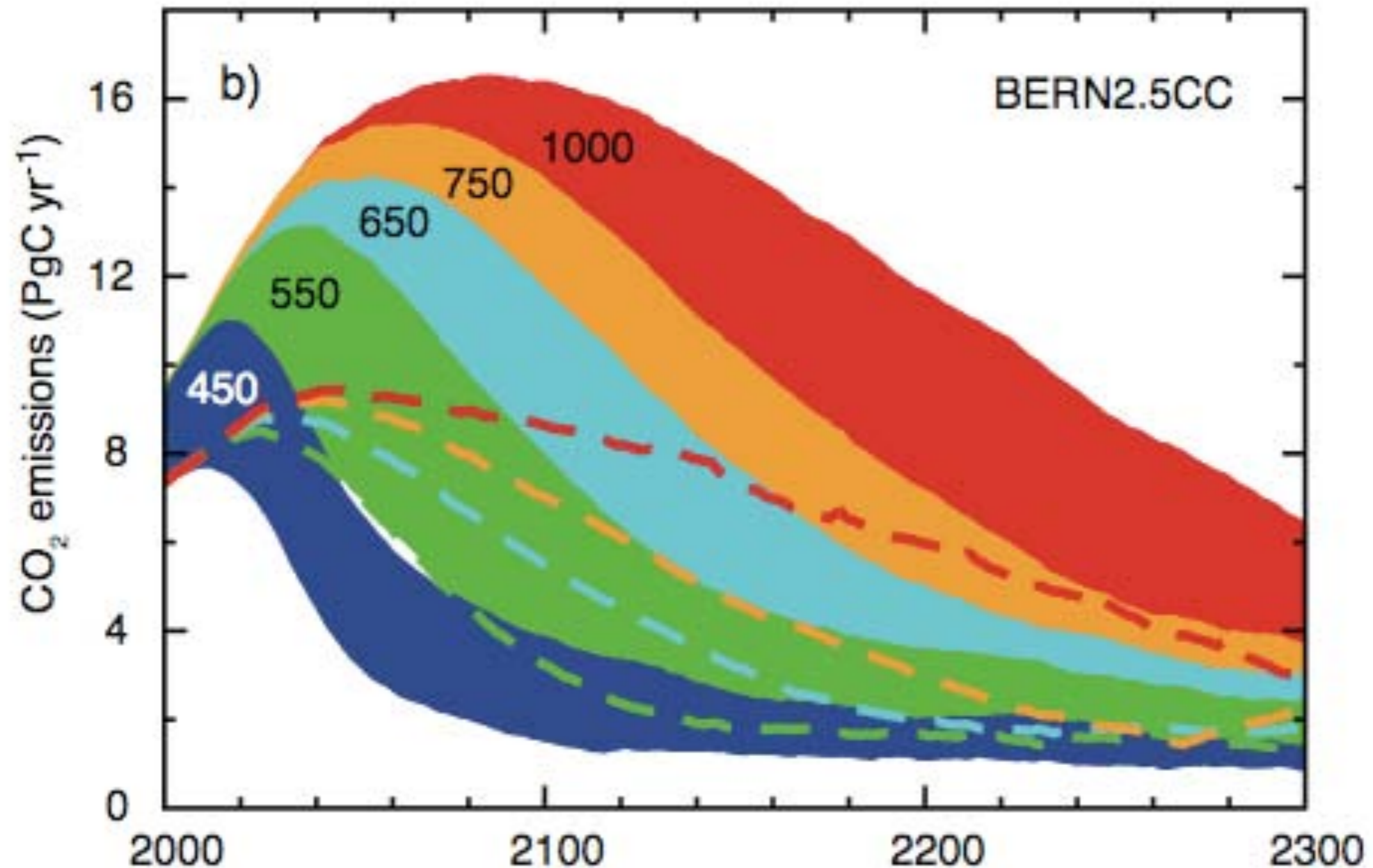
MODIS images from NASA's Terra satellite courtesy of Ted Scambos, National Snow and Ice Data Center, University of Colorado, Boulder.



Surveys show the mountain pine beetle has infested 21 million acres and killed 411 million cubic feet of trees -- double the annual take by all the loggers in Canada. In seven years or sooner, the Forest Service predicts, that kill will nearly triple and 80 percent of the pines in the central British Columbia forest will be dead.

The Washington Post, March 1, 2006

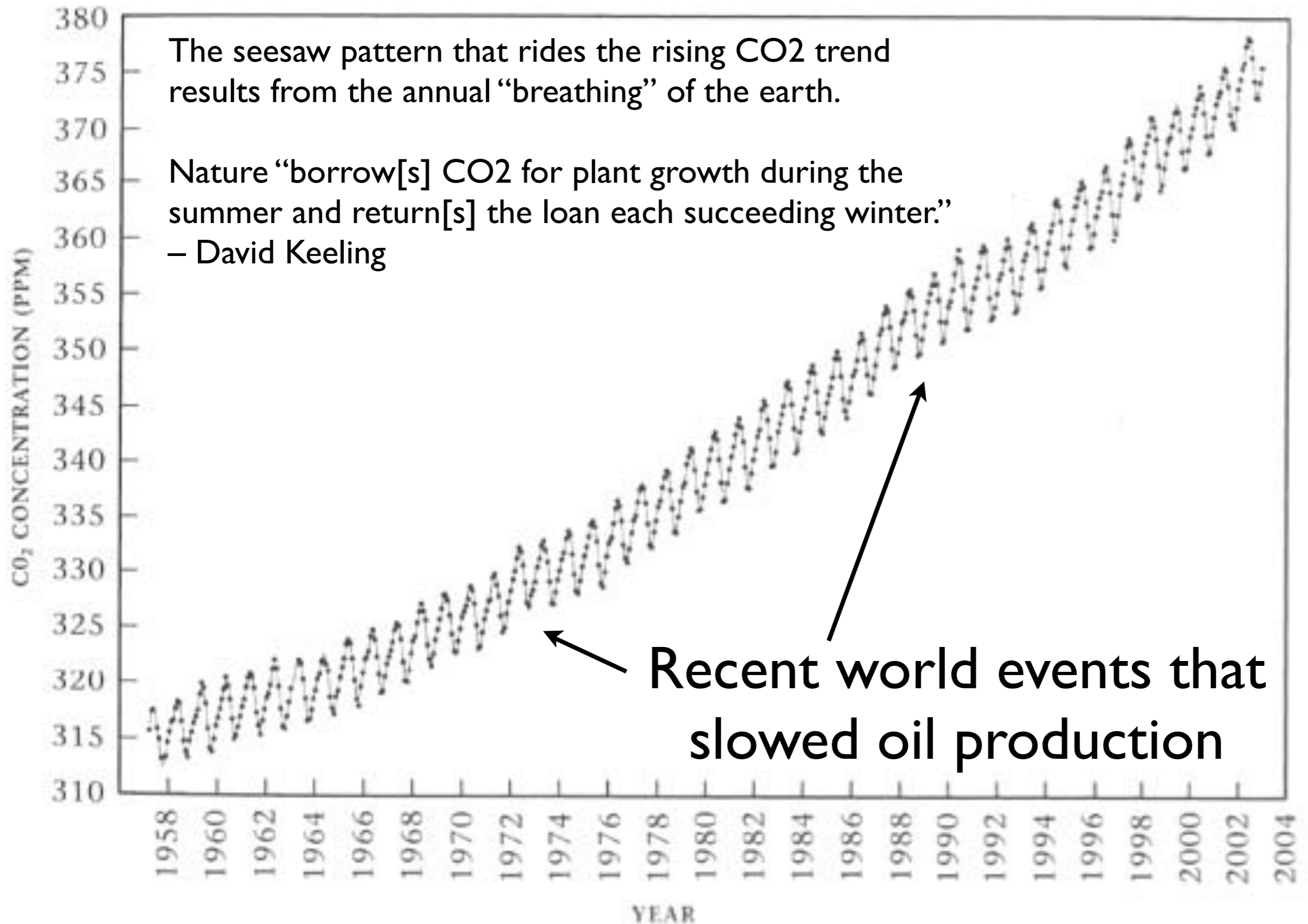
CO₂ Projections



Source: Climate Change 2007: The Physical Science Basis. Contribution of Working Group I to the Fourth Assessment Report of the Intergovernmental Panel on Climate Change

Climate Change 2007: The Physical Science Basis. Working Group I Contribution to the Fourth Assessment Report of the Intergovernmental Panel on Climate Change, Figure 10.22 (b). Cambridge University Press.

MAUNA LOA OBSERVATORY, HAWAII
AVERAGE MONTHLY CARBON DIOXIDE CONCENTRATION



The seesaw pattern that rides the rising CO₂ trend results from the annual “breathing” of the earth.

Nature “borrow[s] CO₂ for plant growth during the summer and return[s] the loan each succeeding winter.”

– David Keeling

Recent world events that slowed oil production

Image by Dr. Pieter Tans, [NOAA/ESRL](#) and Dr. Ralph Keeling, [Scripps Institute of Oceanography](#).

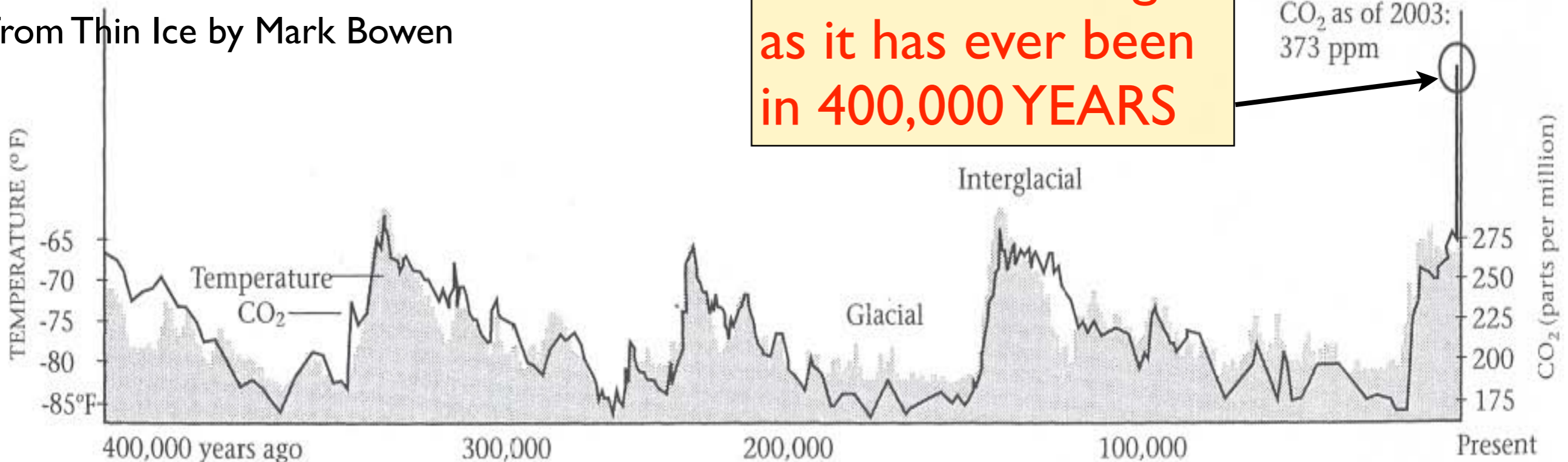


Temperature inferred from isotope ratios in the Vostok ice core

Carbon dioxide levels measured in the trapped air bubbles in the same core

Photo by Lonnie Thompson, Courtesy of Ohio State University. All rights reserved.

from Thin Ice by Mark Bowen



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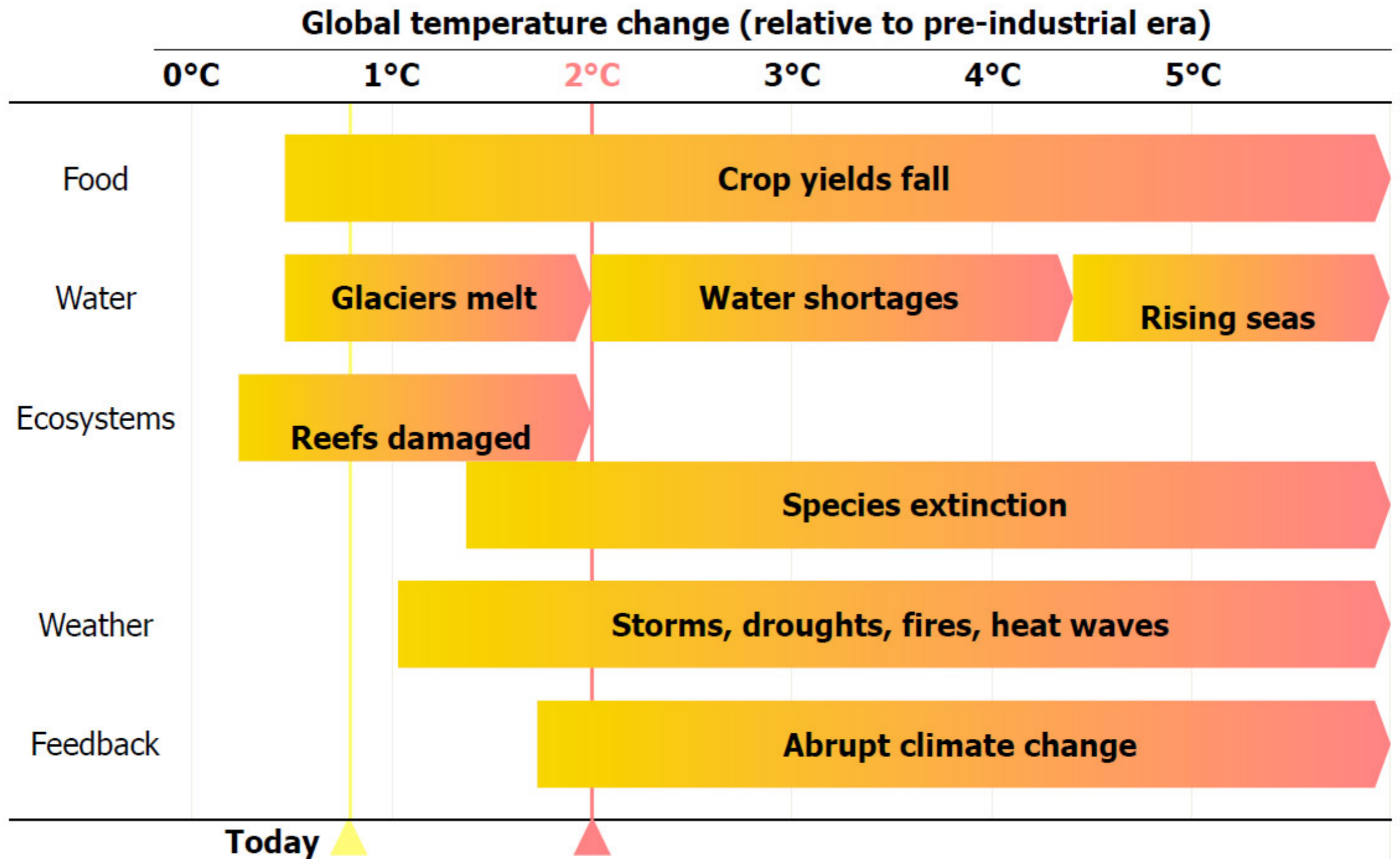
“I can get eight professors from MIT on both sides of this issue and no one in this room will walk away understanding what they said about climate change.”

□ Charlie Baker, Former Candidate for
Massachusetts Governor



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If warming exceeds 2°C, negative effects increase and catastrophic changes become more likely



Courtesy of Hal Harvey. Used with permission.

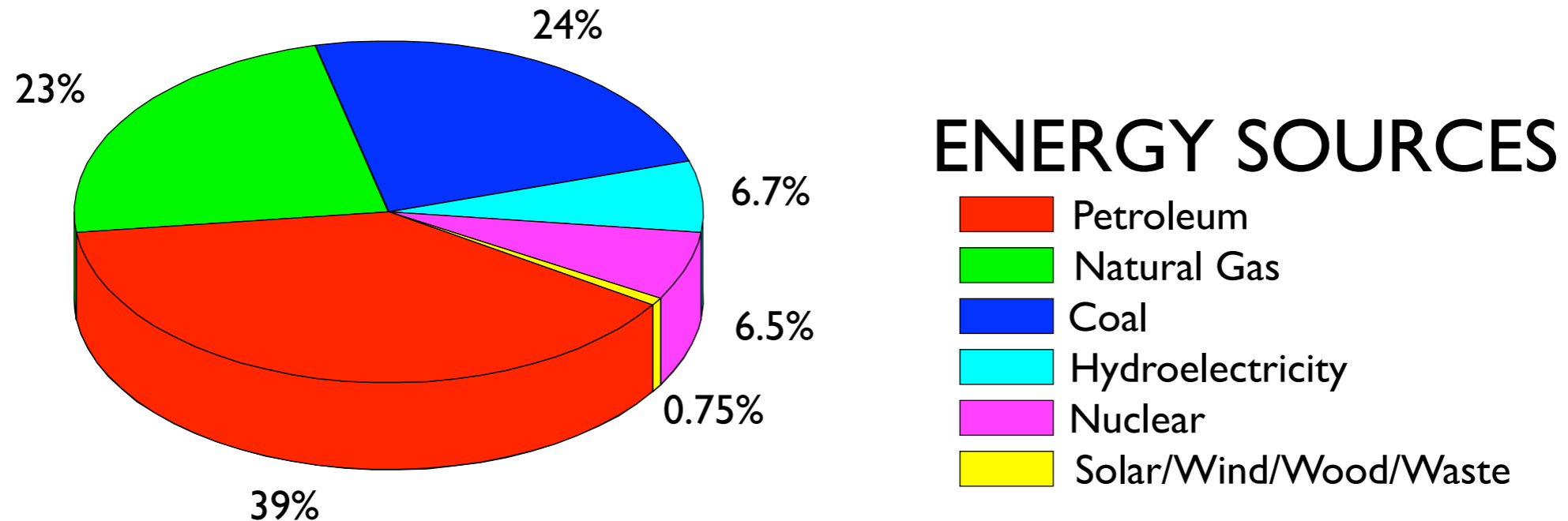
Courtesy: Hal Harvey (Climate Works)

Abundance of Solar Energy

Average solar power incident on Earth ~ 130,000 TW

Global energy consumption (2001) ~ 13.5 TW

Source: DOE



If ~2% of the continental United States is covered with PV systems with a net efficiency of 10% we would be able to supply all the US energy needs (0.3% land coverage to meet just electricity needs)

(Land area requirement is comparable to area occupied by interstate highways)

Note: 40% of our land is allocated to producing food

Nuclear power equivalent is 3,300 x 1 GW nuclear power plants.

(1 for every 10 miles of coastline or major waterway)

Solar Across Scales

Moscone Center: 675,000 W



Residential home: 2400 W



Kenyan PV market:
Average system: 18W



Solar Land Area Requirements

150 Km² solar panels in Nevada would power the U.S. (15% efficient)

J.A. Turner, *Science* 285
1999, p. 687.

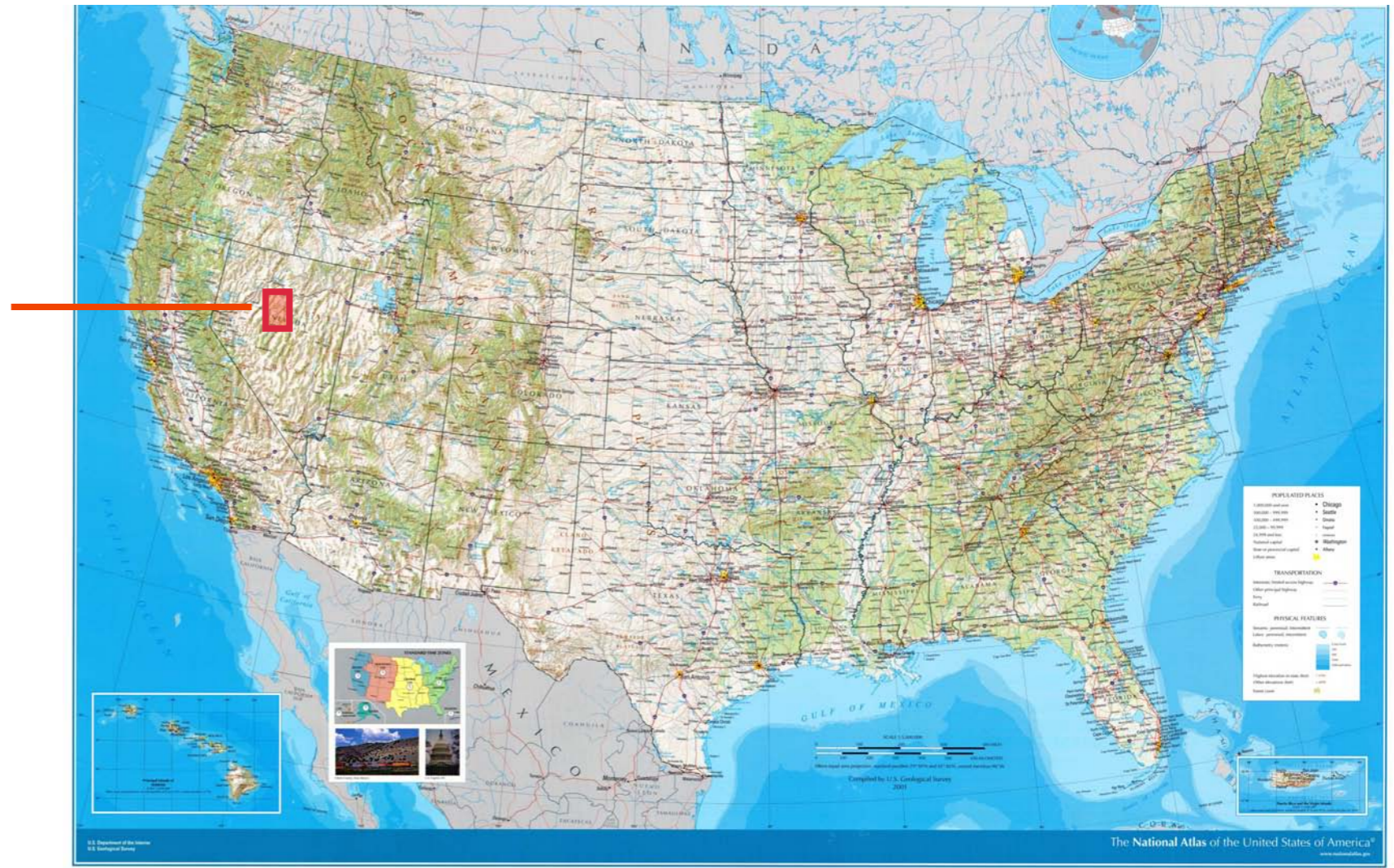
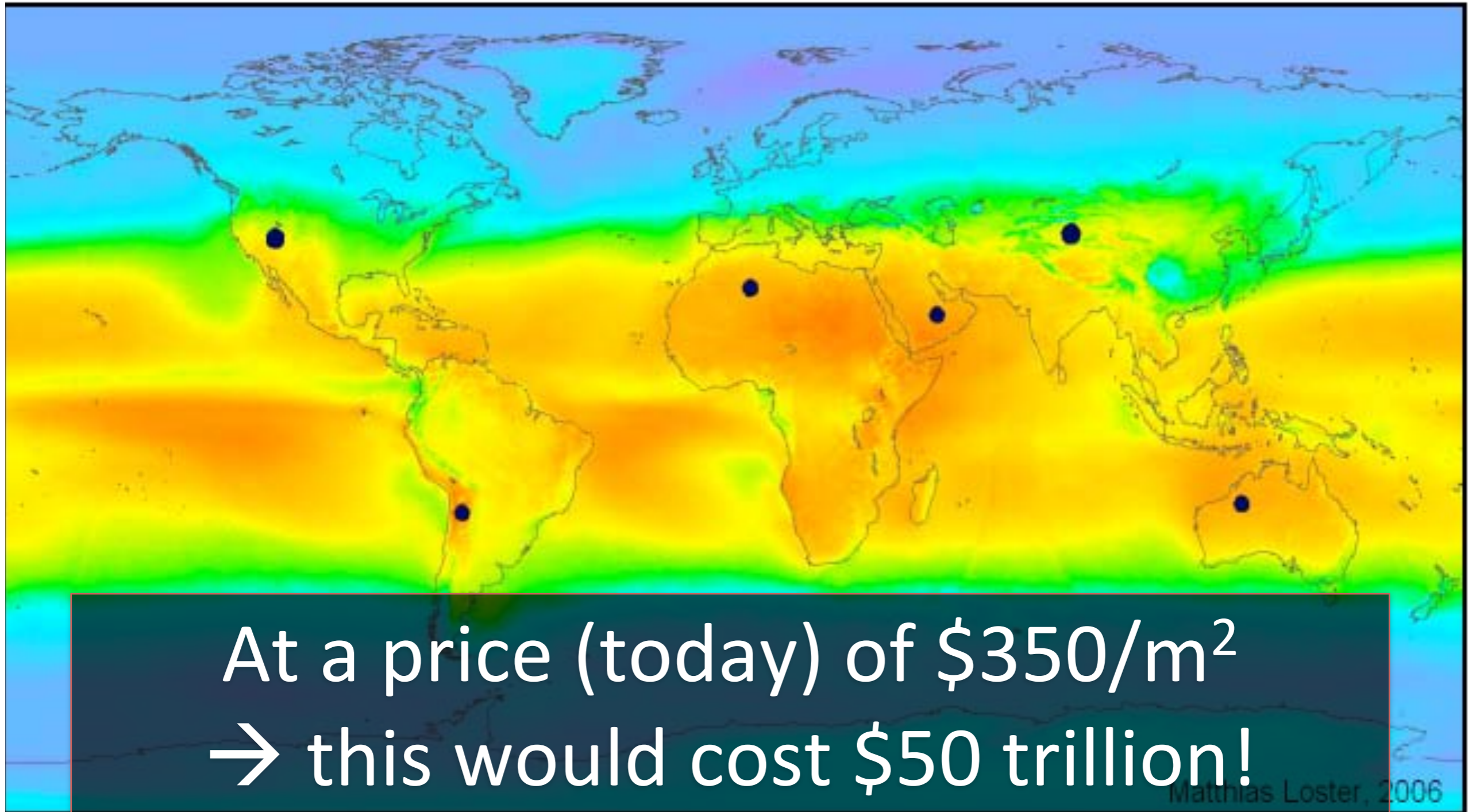


Image by the United States Geological Survey is in the public domain.

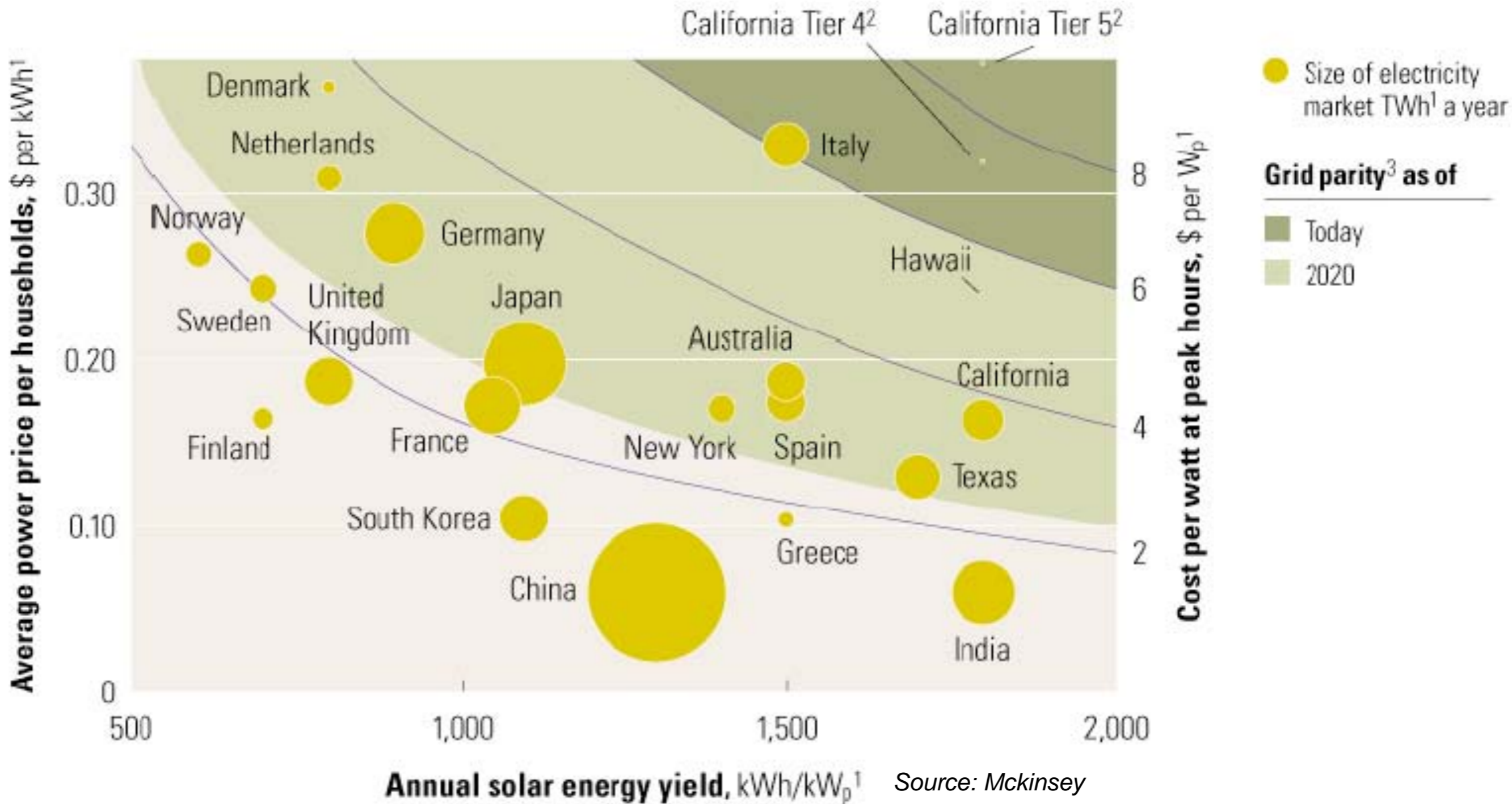
Solar Land Area Requirements for $\sim 20\text{TW}$



At a price (today) of $\$350/\text{m}^2$
→ this would cost $\$50$ trillion!

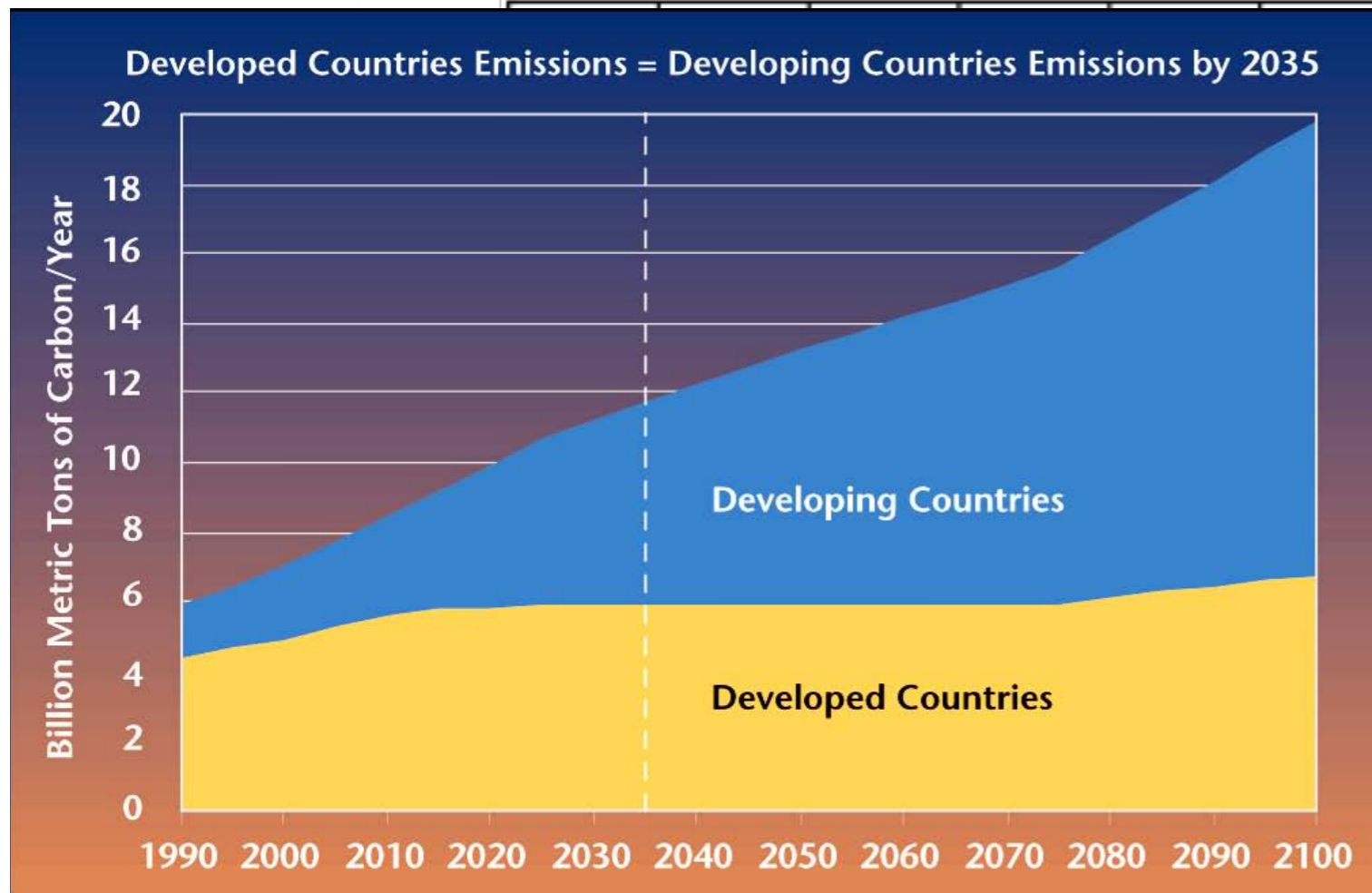
Matthias Loster, 2006

Solar PV: Grid Parity



Lorenz, P., D. Pinner, and T. Seitz. "The Economics of Solar Power." Energy, Resources, Materials: McKinsey & Company, June 2008. All rights reserved. This content is excluded from our Creative Commons license. For more information, see <http://ocw.mit.edu/help/faq-fair-use/>.

Aim: capture 10% of electrical generation with PV



Side note: replacing fossil fuels in the developing world will become much more important in the near future.

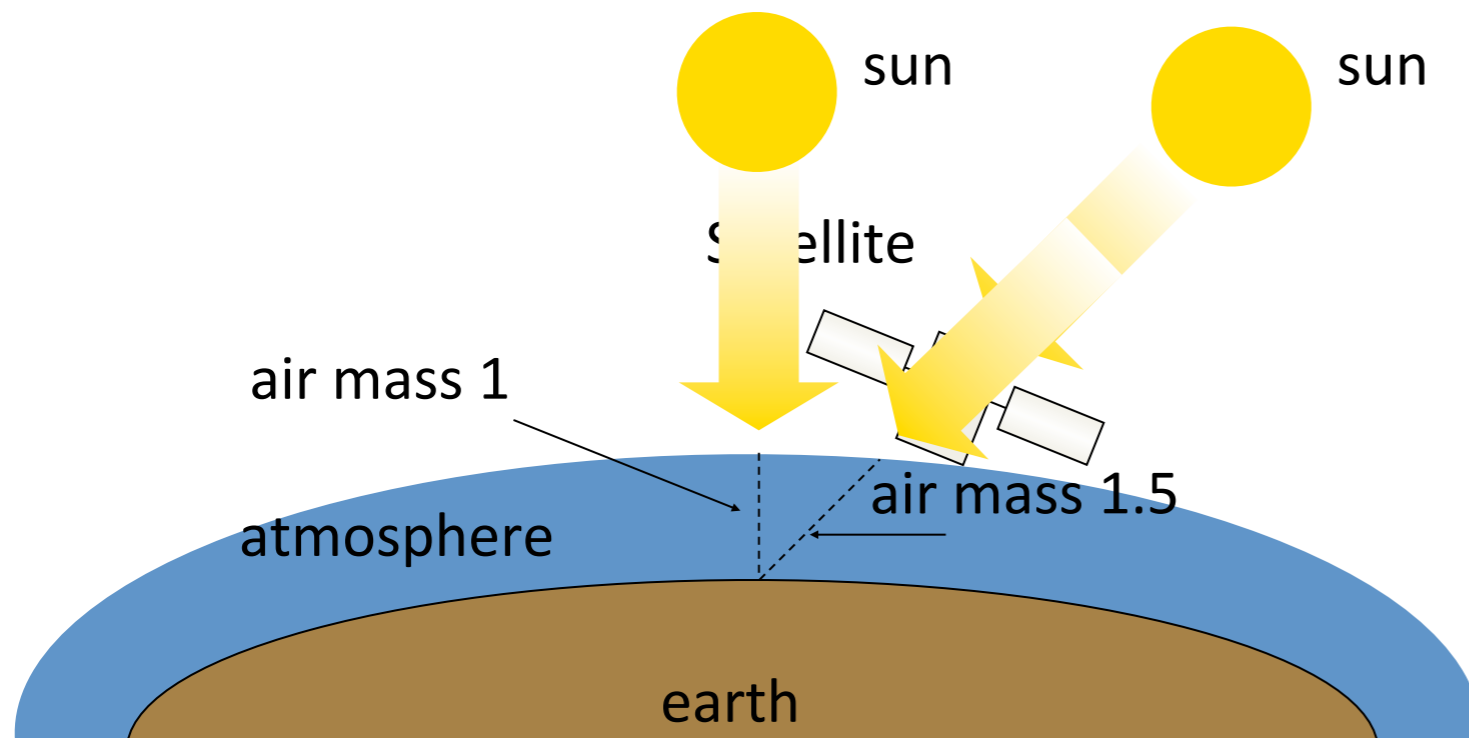
At **14¢ per $kW_e h$** , PV could cost-effectively replace 10% of electrical energy used in U.S.

No storage needed.

Could be deployed by 2022, with 0.04% land use.



SOLAR INTENSITY: HOW MUCH AREA IS REQUIRED TO GENERATE POWER?



Solar spectrum outside atmosphere:
air mass 0 (AM0) 1353 W/m²

At earth's surface:

sun at zenith:

air mass 1 (AM1) 925 W/m²

sun at 45°:

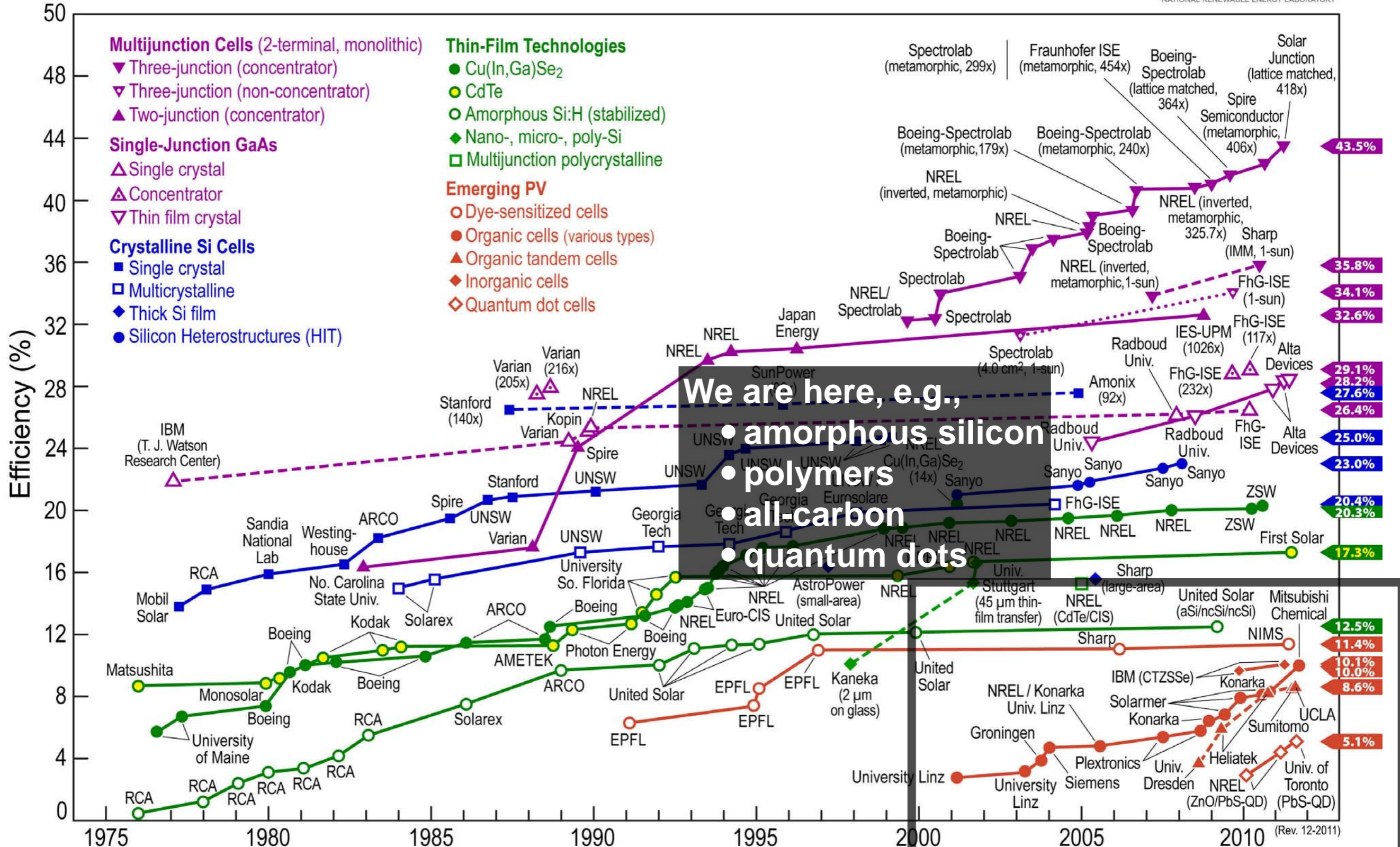
air mass 1.5 (AM1.5) 844 W/m²

AM1.5 is terrestrial solar cell standard

Comparison of PV Technologies



Best Research-Cell Efficiencies



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Solar PV technology landscape (2015)

- Cost/efficiency tradeoff:
- high efficiency modules have lower installation costs
- low efficiency modules have lower module costs

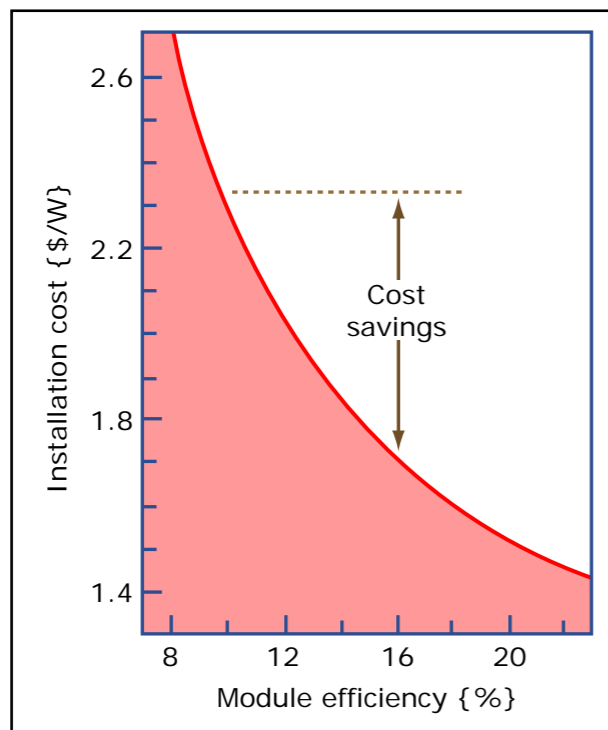
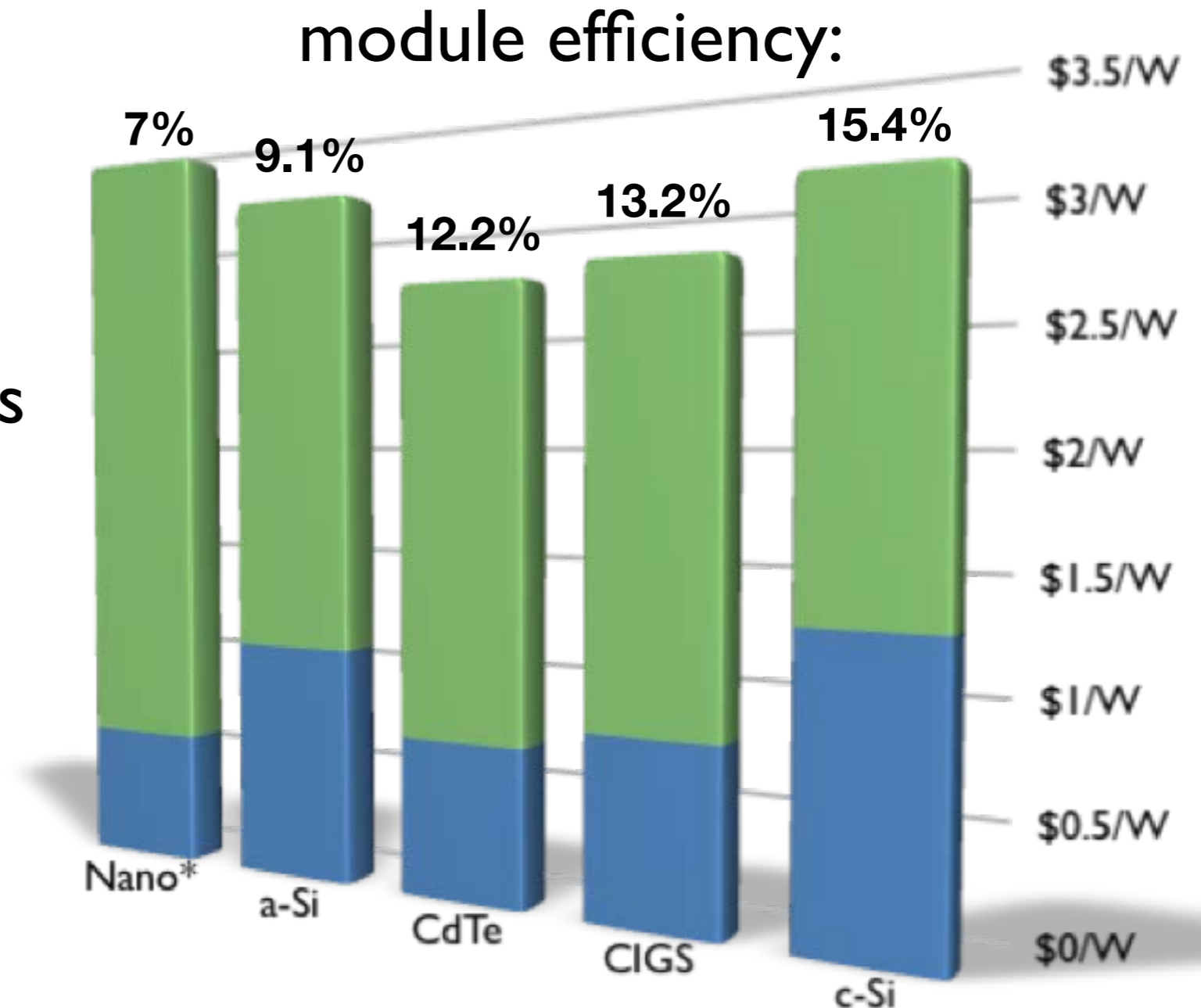


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How do we supply 81 kWh/day/person of solar electricity?

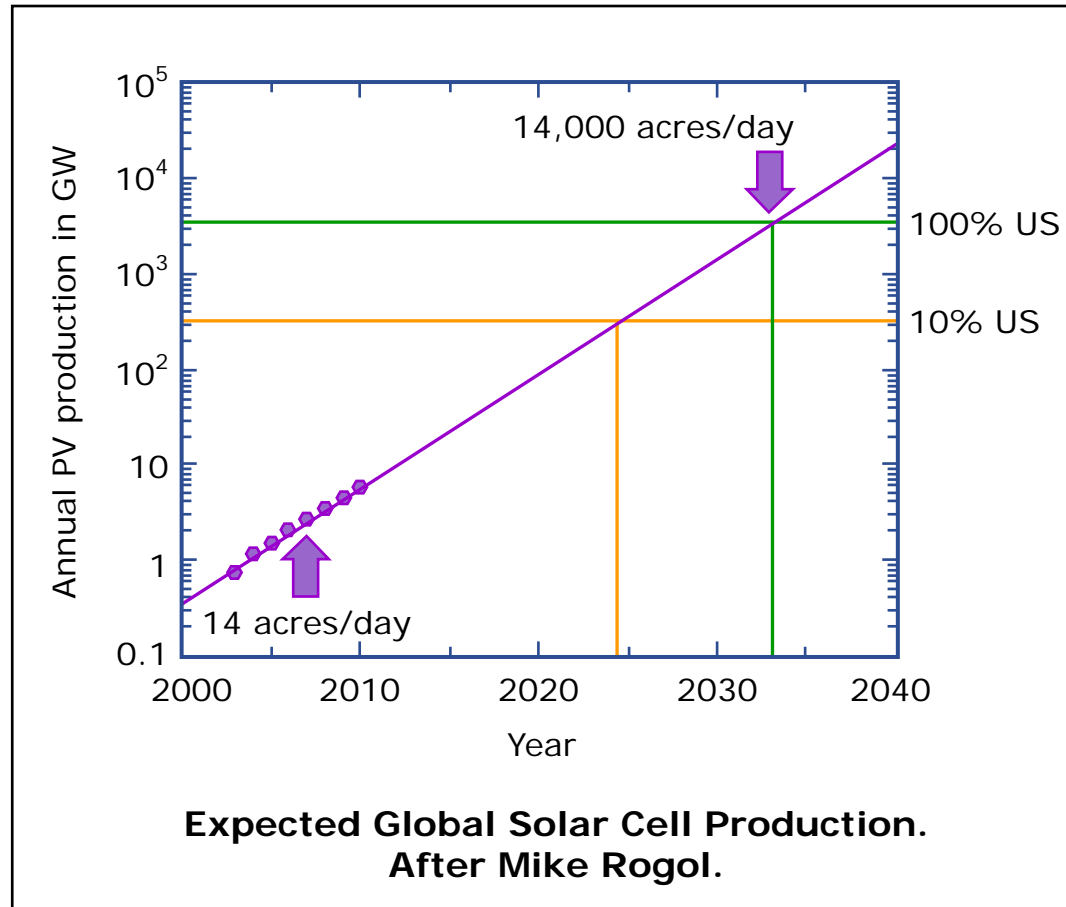


Image by MIT OpenCourseWare.

2006: Solar Cell Production Rate: 14 acres / day

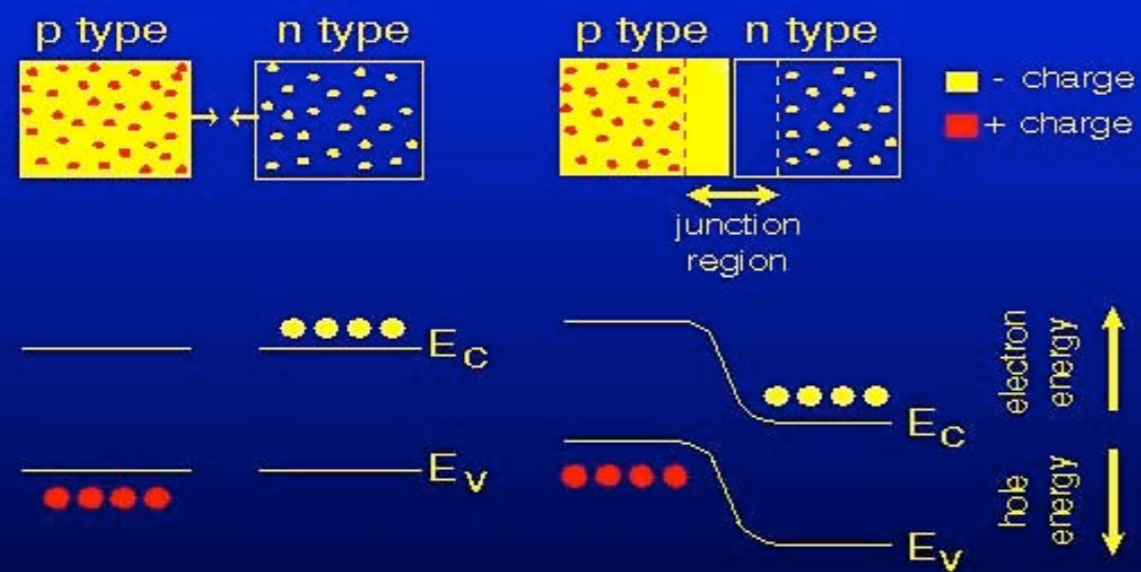
2035: Required Solar Cell Production Rate: 14,000 acres / day

To survive, any new technology needs to:

- ACCELERATE OVER THE Si-PRODUCTION
- REACH HIGHER EFFICIENCIES and/or LOWER INSTALLATION COSTS

PN Junction (brief review)

Diagram of p-n junction formation and the resulting band structure



The diode I-V characteristic

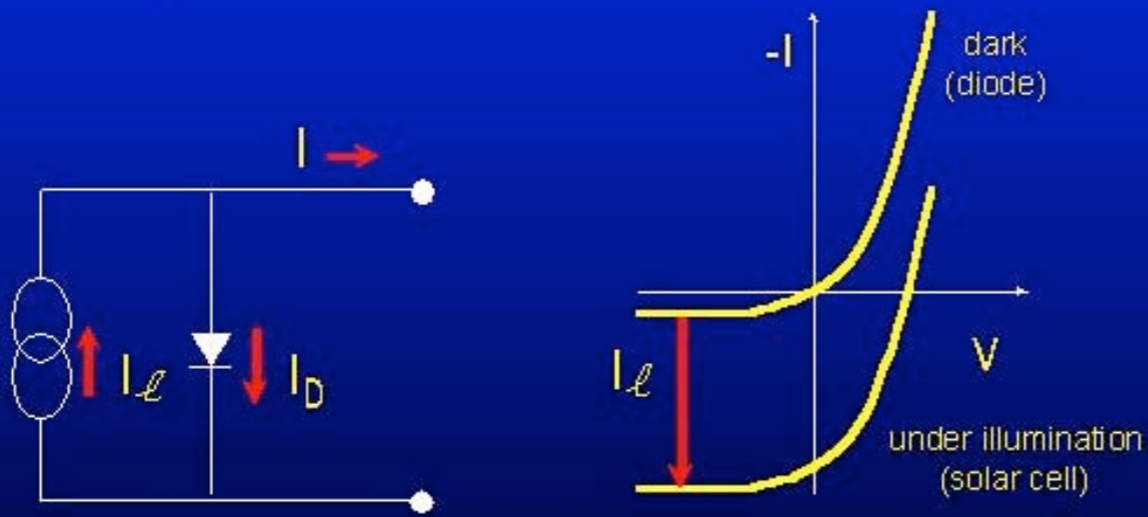


Equilibrium in a p-n junction is still “dynamic” and there are four kinds of currents contributing to the net zero flow of charge.

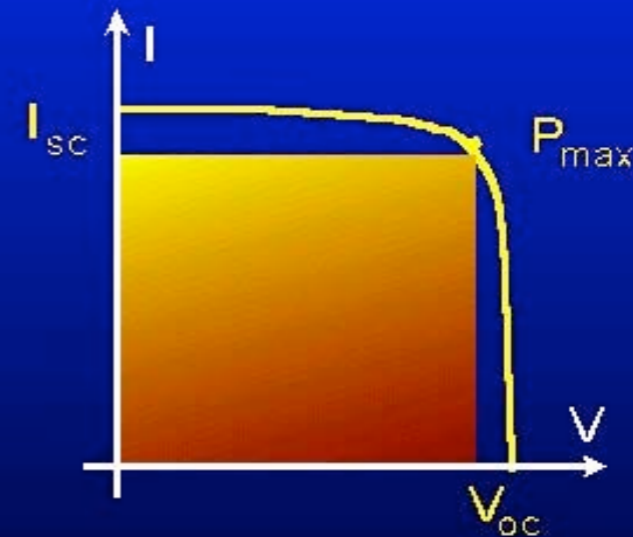
- (1) Majority Hole Current. Diffusional current from hole movement from p to n (current from p to n).
 - (2) Minority Hole Current. Drift current from holes moving from n to p, assisted by the electric field (current from n to p).
 - (3) Majority Electron Current. Electron diffusion from n to p from the high concentration gradient (current from p to n).
 - (4) Minority Electron Current. Electron drift from p to n, assisted by the electric field (current from n to p).
- In reverse bias ($V < 0$), the current comes from minority carriers and is due to drift. In forward bias ($V > 0$), the current arises from majority carriers and is due to diffusion.

PN Junction (brief review)

The equivalent circuit and I-V characteristic of a solar cell compared to a diode



The I-V characteristic of a solar cell with the maximum power point

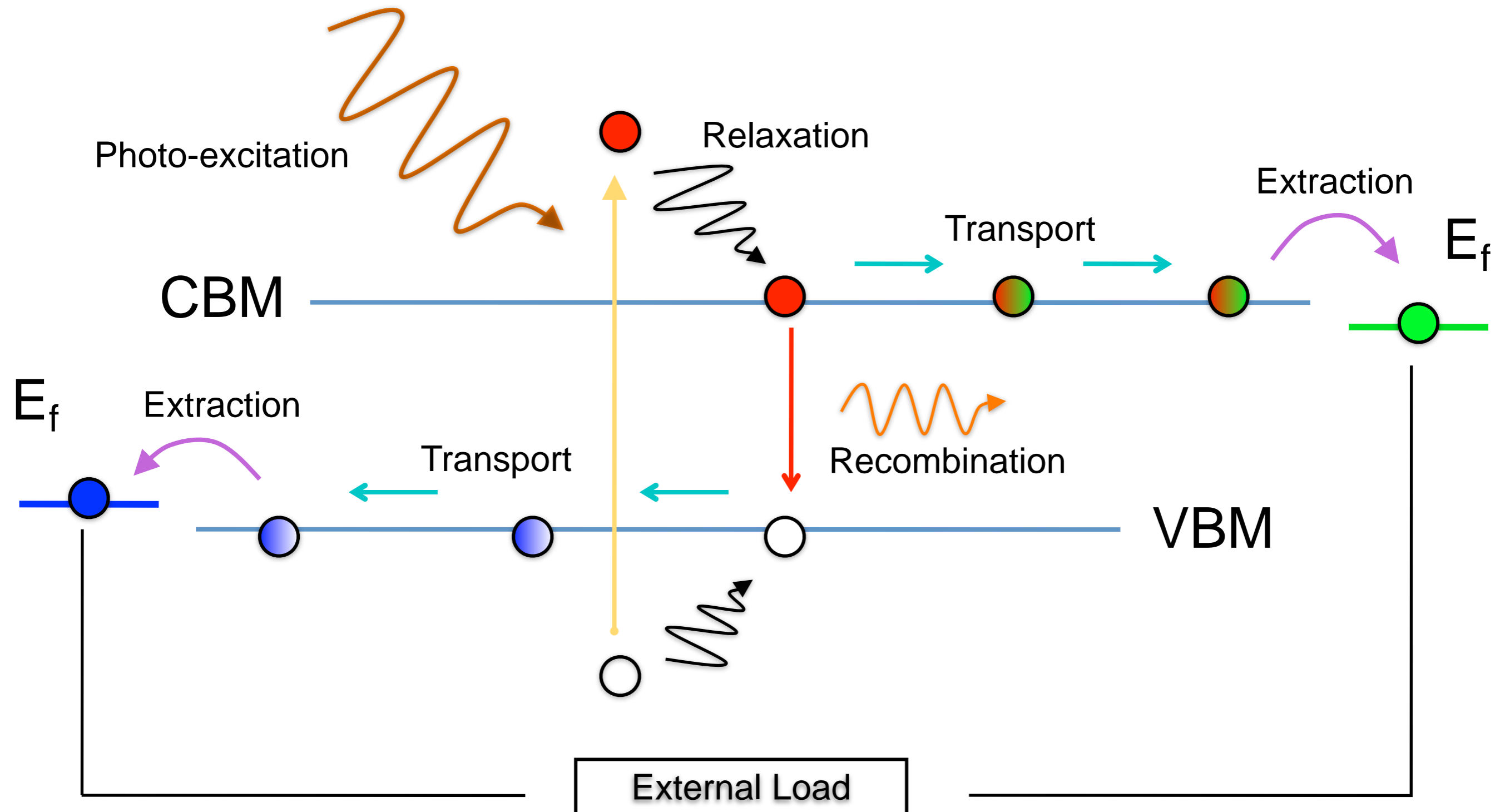


The presence of light induces a net positive change in the generation–recombination rate. Roughly speaking, for each type of current, the effect of light is:

- (1) Majority Hole Current. Relatively unaffected, if generation occurs evenly on both sides.
- (2) Minority Hole Current. Increased, due to the additional carriers now present. The additional carriers resulting from illumination are immediately transferred across the junction in the form of a drift current.
- (3) Majority Electron Current. Relatively unaffected.
- (4) Minority Electron Current. Increased, due to the additional carriers now present.

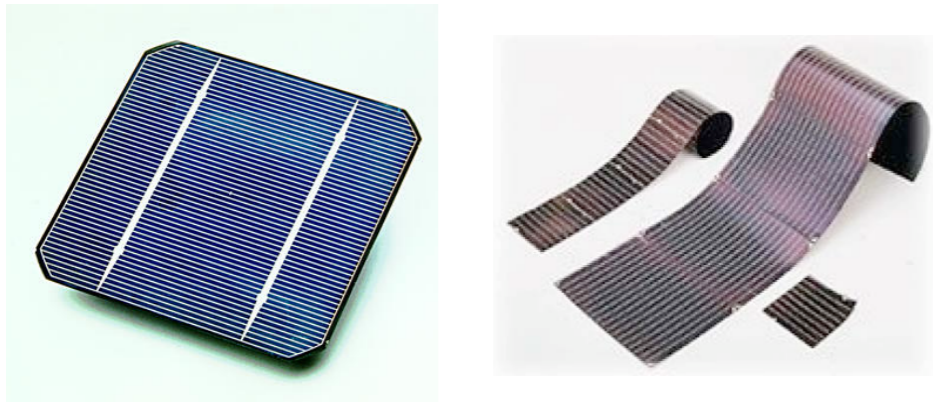
Effectively, under illumination, the IV characteristic of the PN junction is shifted downwards, by an amount that is directly determined from the photocurrent incident upon the junction.

Fundamental Processes Involved in Solar Photovoltaics: Electron's View

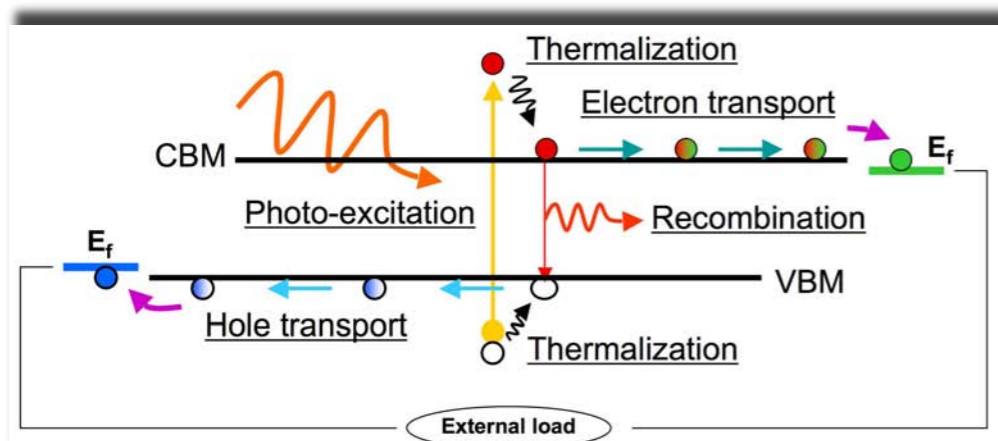


The Role of Computational Quantum Mechanics

- What do we know how to compute?
- How does it help for solar PV?



Images of solar panel and strips © sources unknown. All rights reserved. This content is excluded from our Creative Commons license. For more information, see <http://ocw.mit.edu/help/faq-fair-use/>.



?
electrical
properties

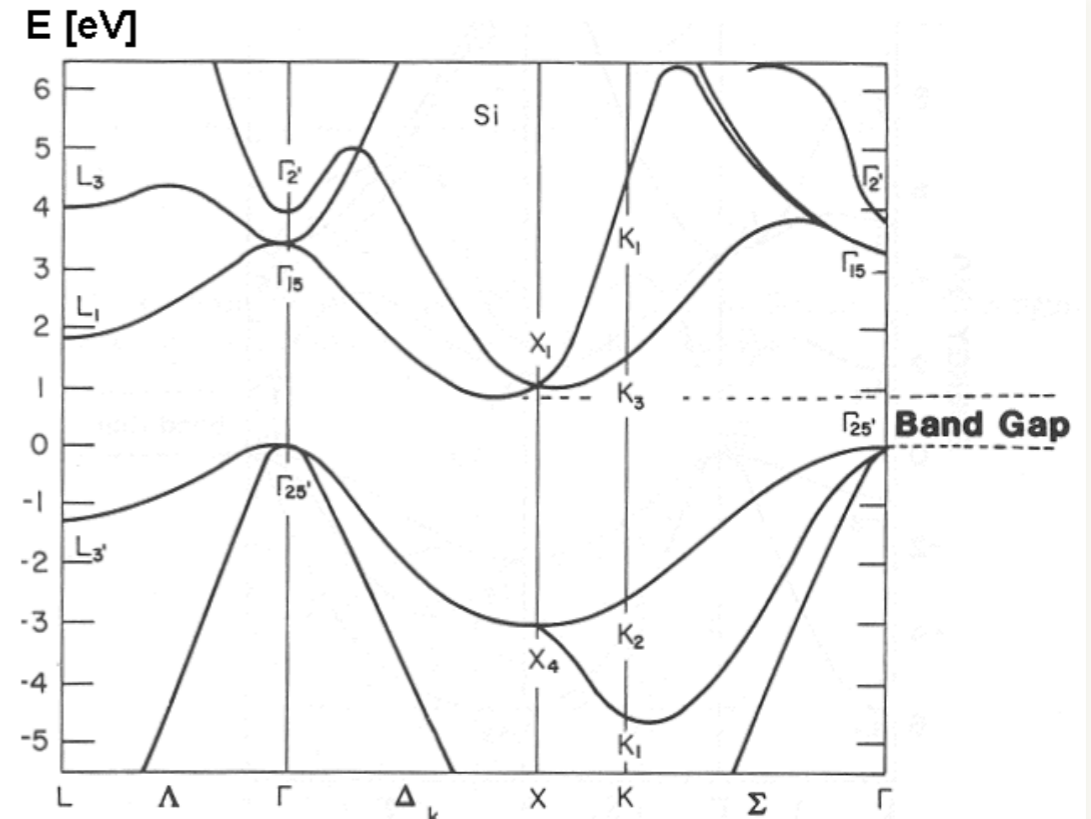


?
mechanical
properties

?
optical
properties

Crystalline Silicon Solar PV (80% of current market)

- Light Absorption
 - Band Gap
 - Band Structure
- Electron/Hole Transport
 - Electron/Hole Mobilities



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$$\sigma = e^2 \tau \int \frac{d\mathbf{k}}{4\pi^3} \left(-\frac{\partial f}{\partial E} \right) \mathbf{v}(\mathbf{k}) \mathbf{v}(\mathbf{k})$$

Amorphous Silicon Solar PV (3% of current market)

- Light Absorption (is actually pretty good)
- Electron-Hole Separation (also not a problem)
- Electron/Hole Transport (Holes are Slow!)
 - Hole Mobilities
 - Hole Traps: from total energy differences
($E_{\text{neutral}} - E_{\text{charged}}$)

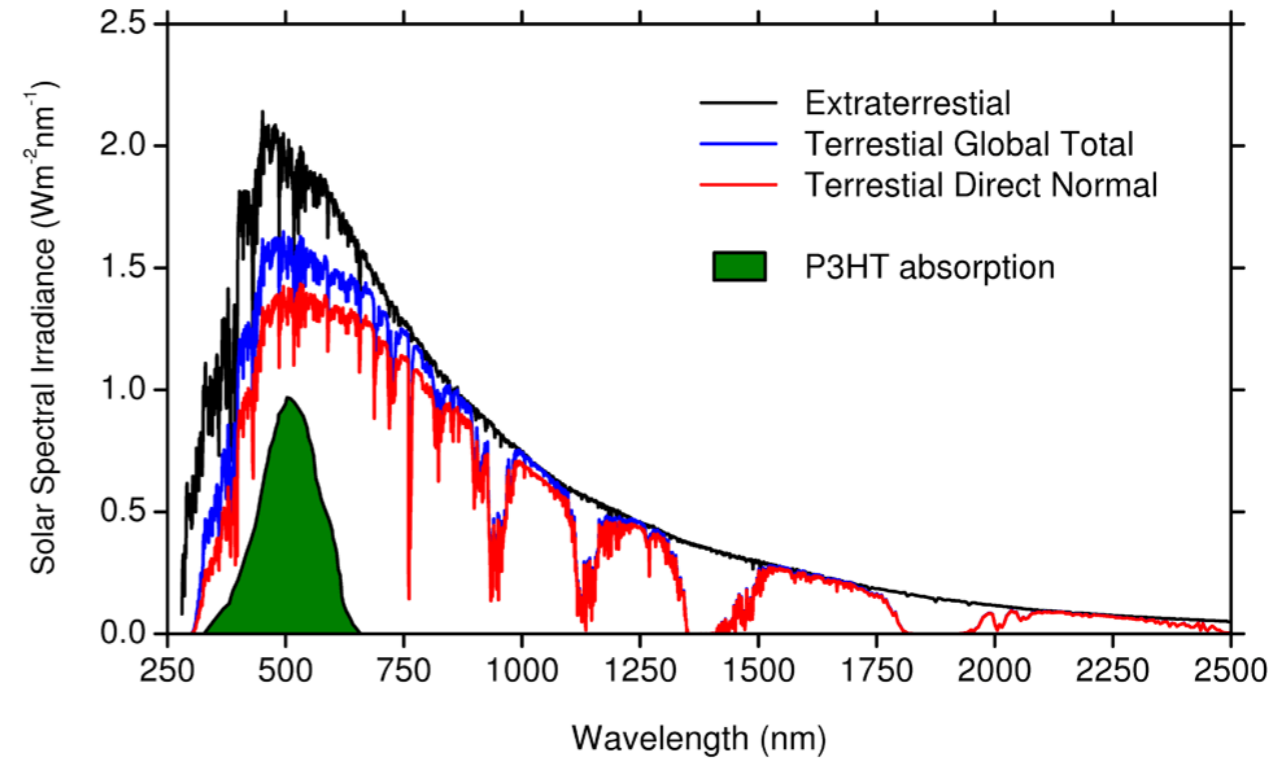
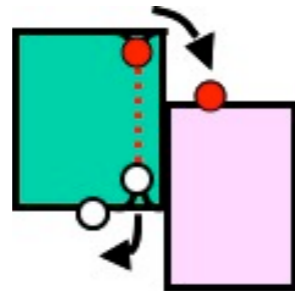
Organic Solar PV

- Light Absorption (need to capture more of the solar spectrum)

- Band gap

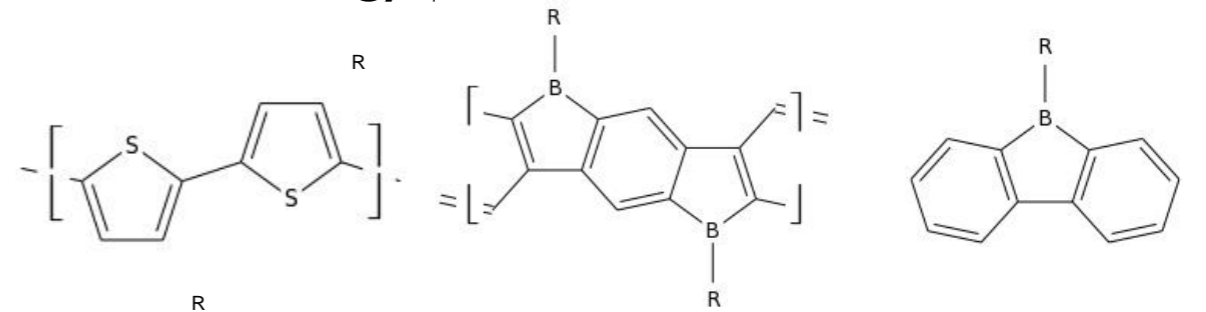
- Electron-Hole Separation

- Orbital energies



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Poly(3-hexylthiophene) (P3HT): $E_{g,exp} = 2.1 \text{ eV}$
 Low-energy photons are not absorbed!



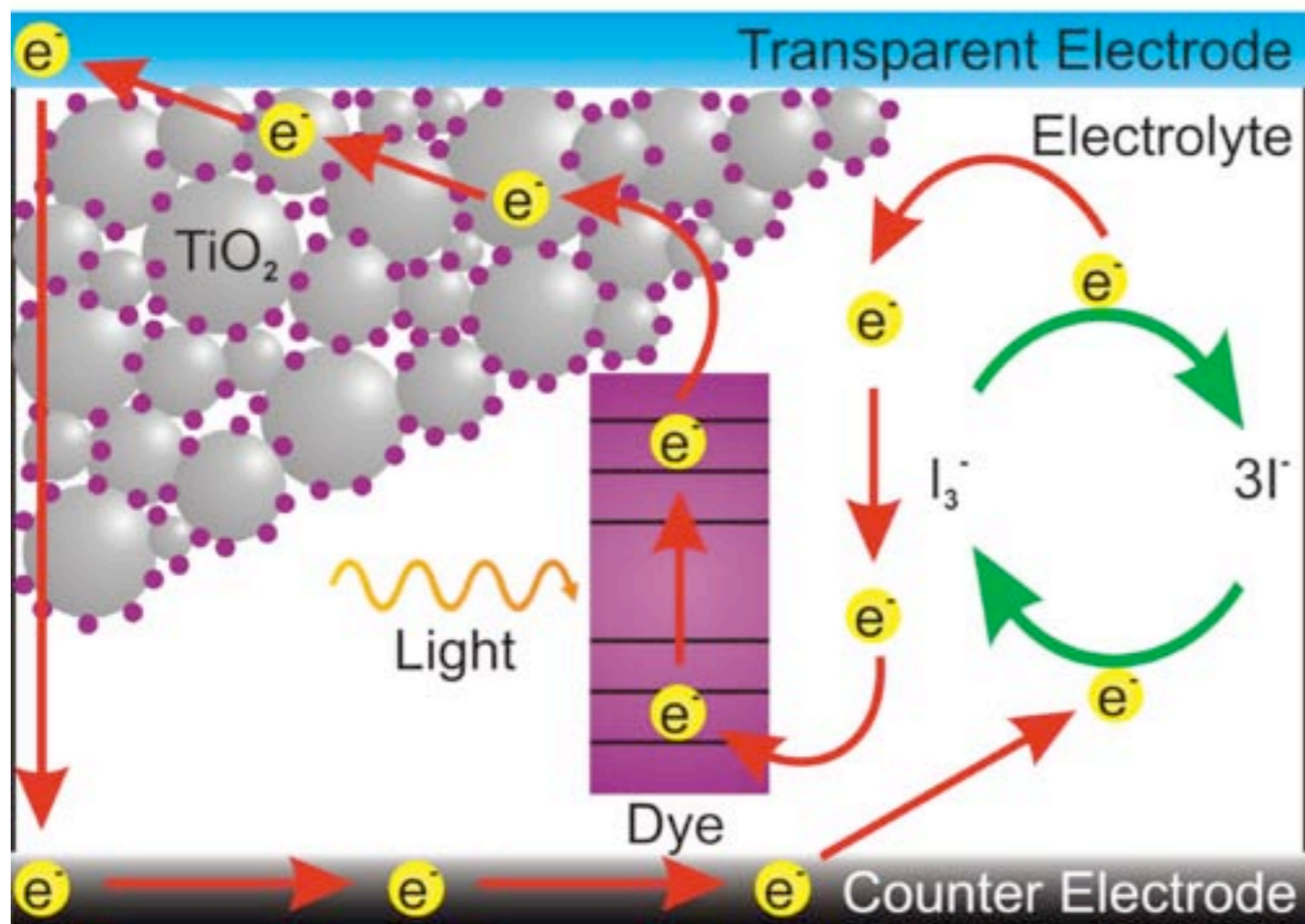
$$E_{gap} = E_0$$

$$E_{gap} = 0.55E_0$$

$$E_{gap} = 1.1E_0$$

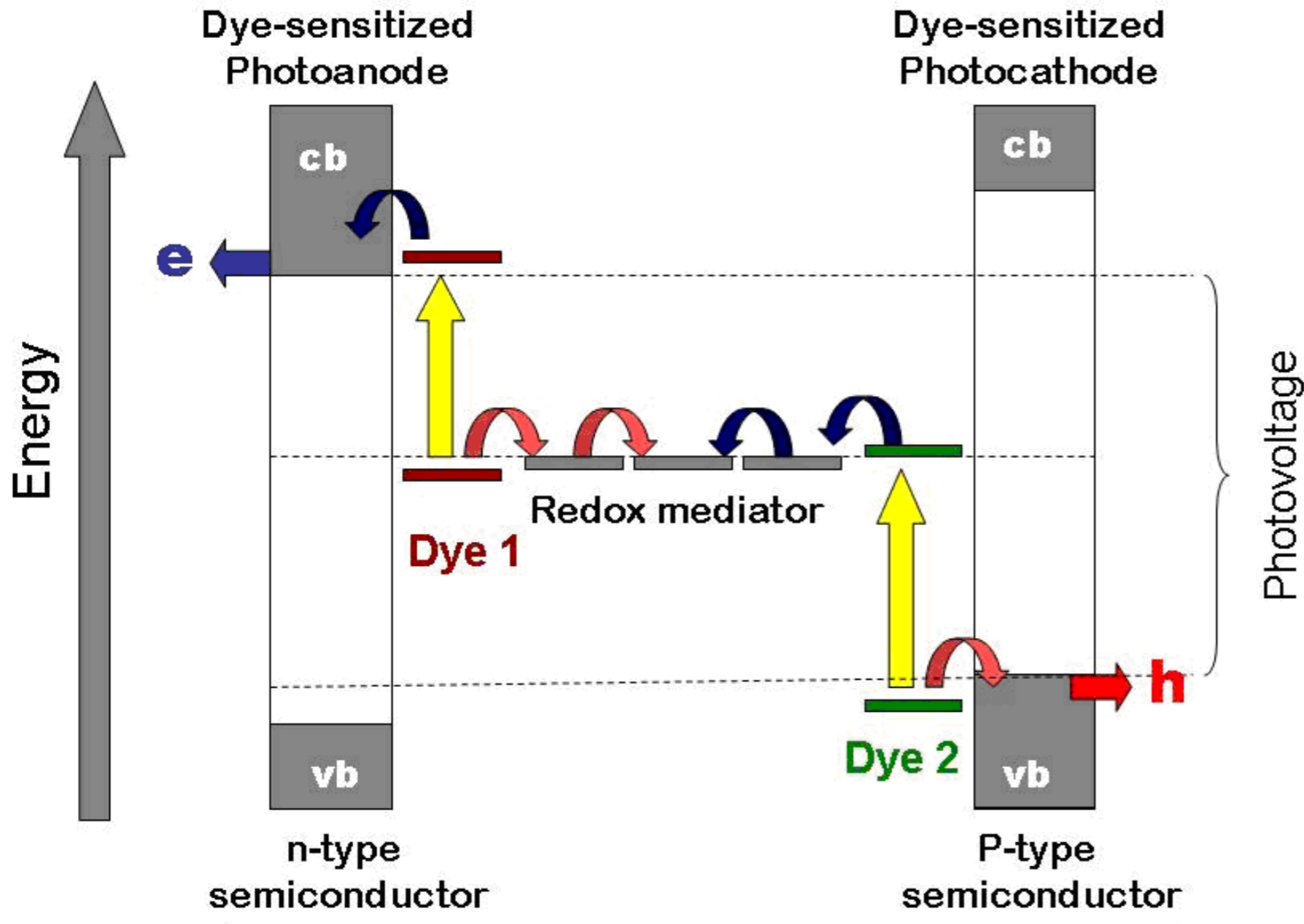
Dye Sensitized Solar PV


Gratzel and O'Regan
(Nature, 1991)




- Made up of 3 active materials:
- **Dye** absorbs light.
 - **TiO₂ nanoparticles** with very large surface area take electron.
 - Liquid **electrolyte** delivers new electron from cathode to dye.

Dye Sensitized Solar PV



 = electron transfer step

vb = valence band

 = hole transfer step

cb = conduction band

- Biggest problem is a liquid electrolyte.
- **Relative energy levels** of TiO₂ and dye also key.

Summary

- Energy is a Major Global Challenge
- The Sun has a Lot of it For Free but it's Too Expensive to Utilize
- Computational Quantum Mechanics can Help us **Understand** and **Predict** PV New Materials

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